

The University of Waikato
Department of Mathematics

Topics in Pure Mathematics: Topology, math319-11A
Assignment 2s, due Friday 27th May - through the slot
outside G3.19.

1. If X is a set and A, B subsets show that $X \setminus A \cup B = (X \setminus A) \cap (X \setminus B)$.

2. If $X = \{a, b, c\}$ and $\tau = \{\emptyset, \{a, b, c\}, \{b\}, \{a, b\}, \{c, b\}\}$ show that τ is a topology on X . Then show it is not Hausdorff.

3. Show that if \mathbb{R} has its usual topology (with a base of open intervals) then every open subset can be written as an at most countable union of disjoint open intervals.

4. If $X = \mathbb{R}^2$ and we define $d((x, y), (a, b)) = |x - a| + |y - b|$ show that d is a metric on X by verifying $M1, M2, M3$. Then describe the ball $B((2, 2), 1)$.

5. Show that the metric $d(x, y) = |x - y|$ generates the usual topology on \mathbb{R} .

6. Show that in the usual topology \mathbb{Q} is dense in \mathbb{R} .

7. If $A \subset X$ and (X, τ) is a topological space show that $A^\circ = A \setminus \partial A$.

8. If $f : X \rightarrow Y$ is a function and $A \subset X$ show that $A \subset f^{-1}(f(A))$.